

**INTRO TO HIGHER MATH**  
**HOMEWORK 5 DUE OCTOBER 10**

- (1) Exercise 3.20 in text
- (2) Exercise 3.24 in text
- (3) Let  $P_k = \{\text{primes } p \in \mathbb{N} \mid p \equiv k \pmod{3}\}$ .
  - (a) Give an explicit description of  $P_0$ .
  - (b) Prove that  $P_2$  is infinite. (Hint: By way of contradiction, assume that  $P_2 = \{p_1, p_2, \dots, p_n\}$  is finite. Consider the number  $3p_1p_2 \dots p_n + 2$ .)
  - (c) One might hope to similarly prove that  $P_1$  is infinite. Explain why the method of proof in part (b) will not work.